Why is the modular group extremal?

In dimension 2, the most famous discrete group of hyperbolic isometries is the modular group $PSL(2,\mathbb{C})$. We explain in what sense it is extremal and determine all discrete groups in dimensions $n \leq 9$ having the same extremal property.